

# Hierarchical structural model of primary visual cortex

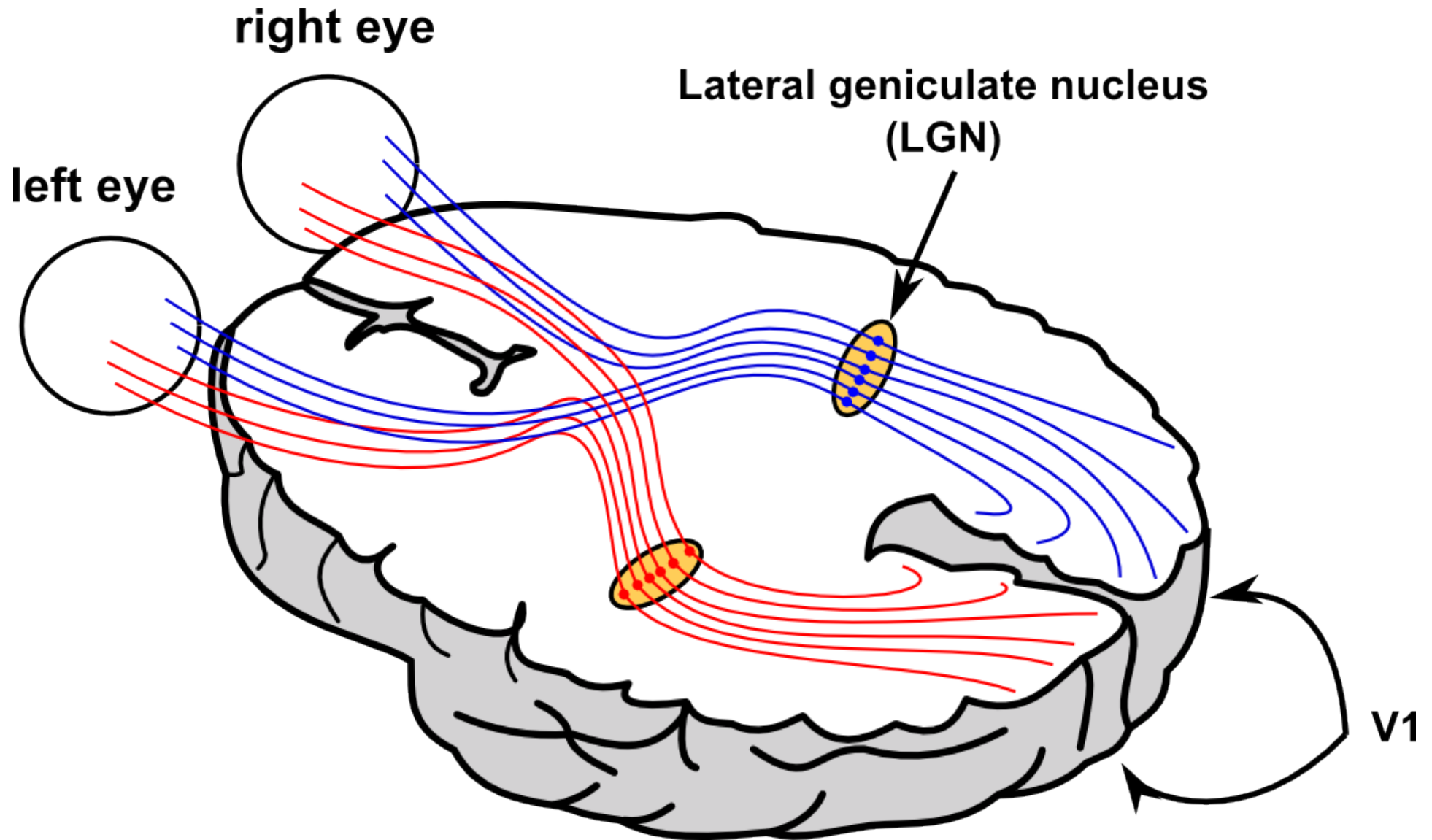
**Ján Antolík**



EUROPEAN UNION  
European Structural and Investment Funds  
Operational Programme Research,  
Development and Education

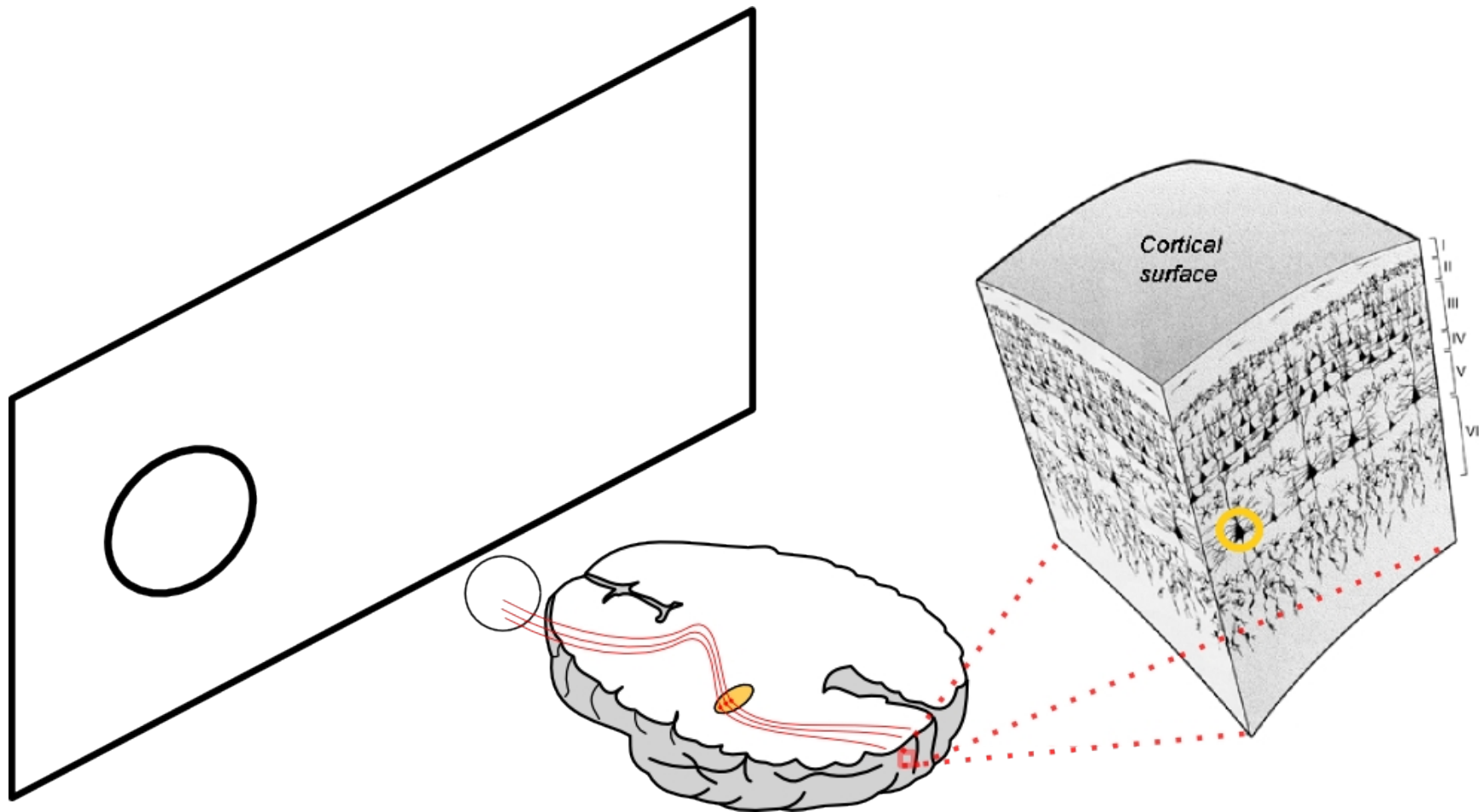
**ME**  
**MT**  
MINISTRY OF EDUCATION,  
YOUTH AND SPORTS

# Early visual system



How do neurons in primary visual cortex process visual information?

# RF: position in visual field

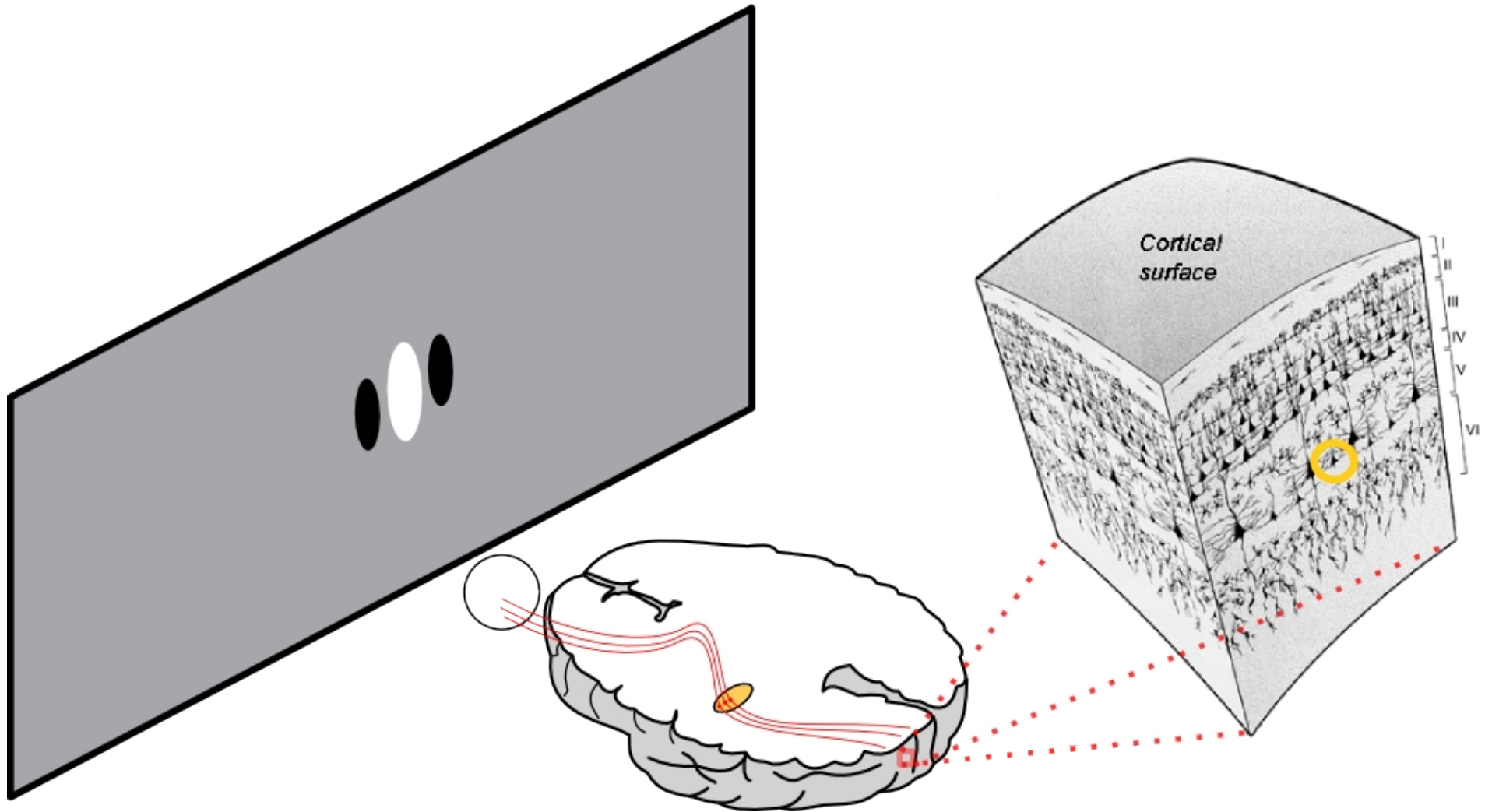


*Responses can be obtained in a given optic nerve fiber only upon illumination of a certain restricted region of the retina, termed the receptive field of the fiber.*

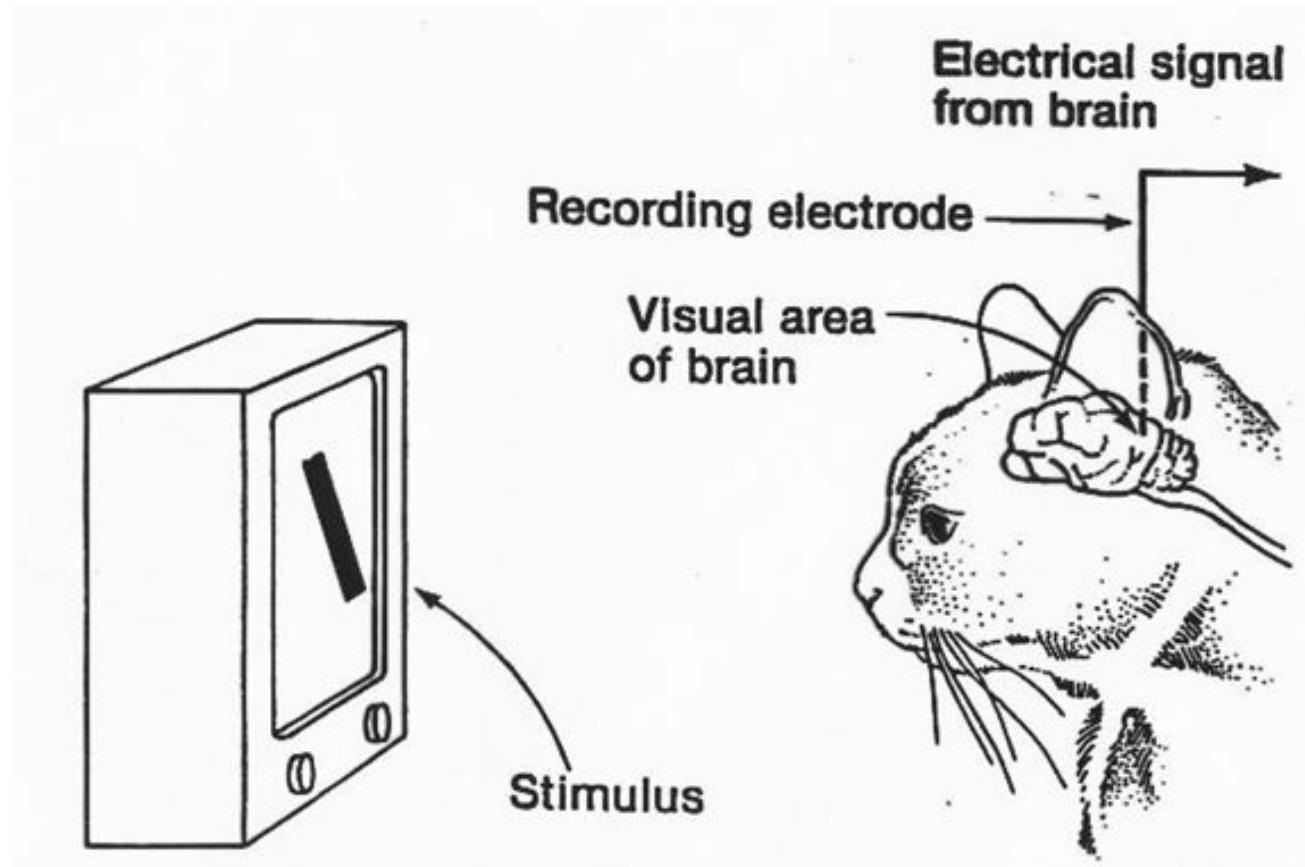
Hartline, H K (1938)



# RF: map of exc/inh regions

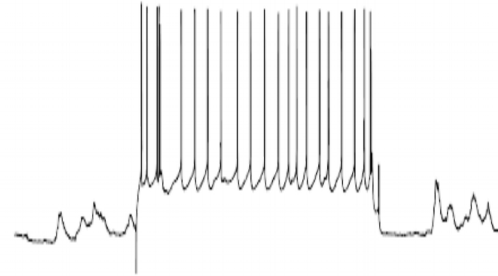
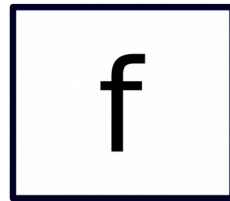


# Receptive Field Estimation

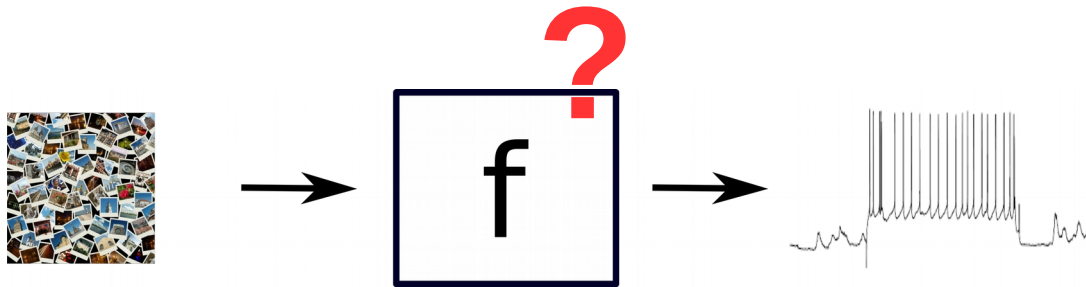


# RF as a function

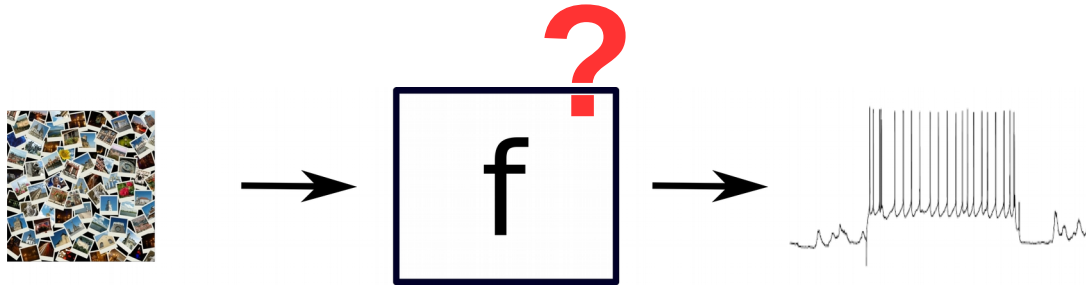
$$f: I^n \rightarrow (0,1)$$



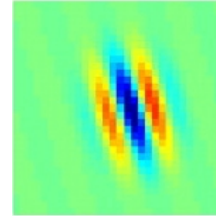
# RF estimation



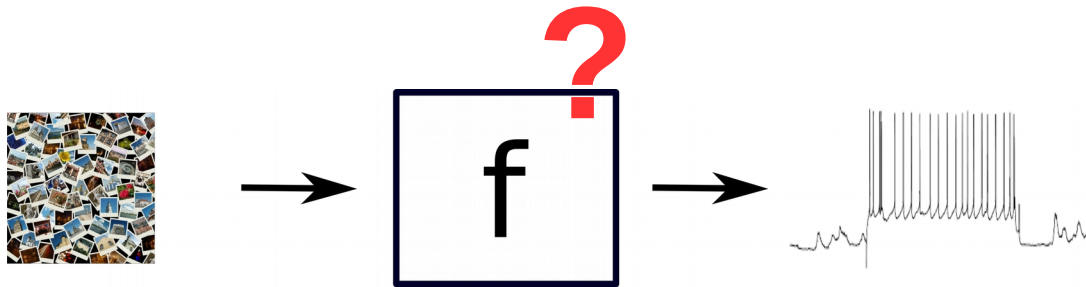
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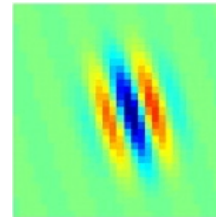
Spike triggered averaging :



# RF estimation



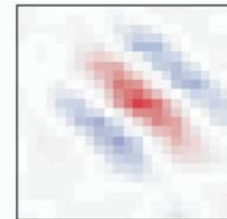
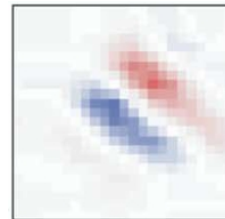
Spike triggered averaging :



1<sup>st</sup> eig. vec.

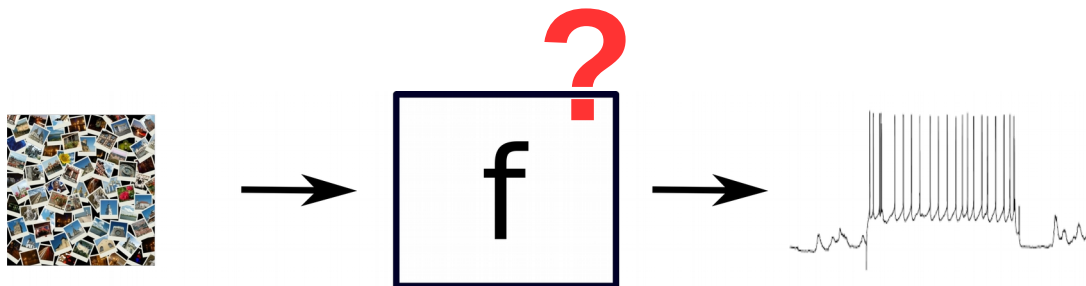
2<sup>nd</sup> eig. vec.

Spike triggered covariance :

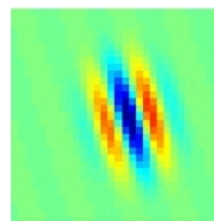


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# RF estimation



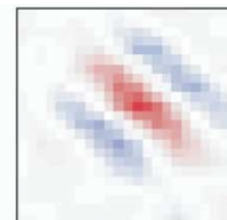
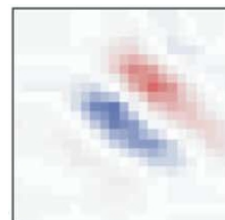
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Spike triggered covariance :

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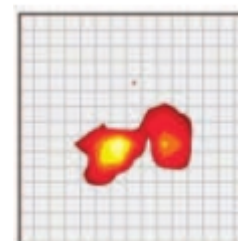
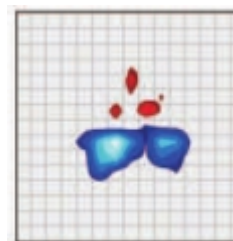


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Volterra kernel estimation :

1<sup>st</sup> order

2<sup>nd</sup> order



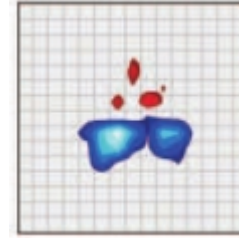
# Is RF real ?

Volterra kernel estimation :

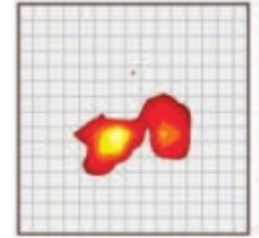
Stimulus



1<sup>st</sup> order



2<sup>nd</sup> order

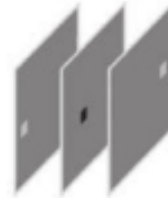




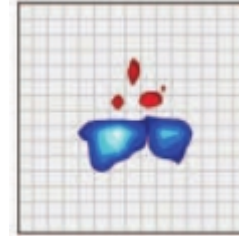
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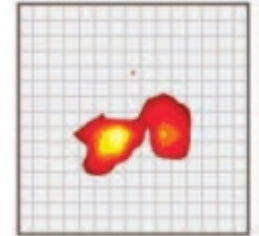
Stimulus



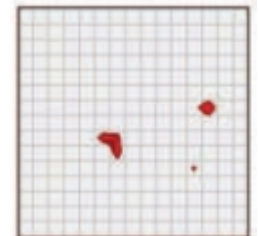
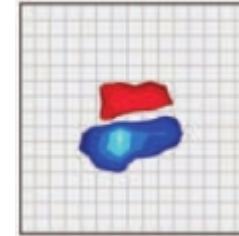
1<sup>st</sup> order



2<sup>nd</sup> order



Volterra kernel estimation :



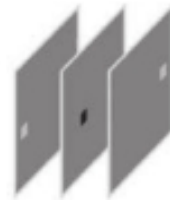
(Fournier et al, 2011)

(David et al, 2004)

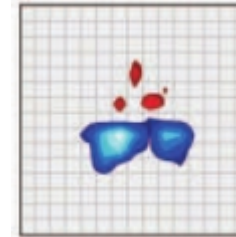
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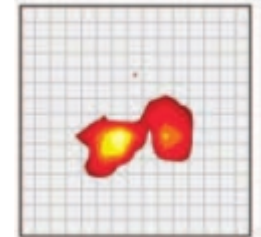
Stimulus



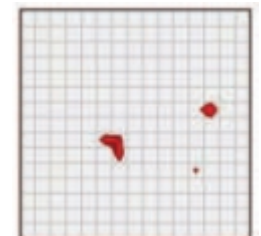
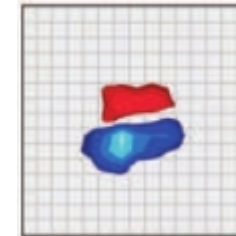
1<sup>st</sup> order



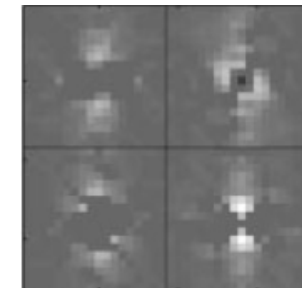
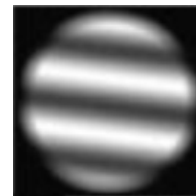
2<sup>nd</sup> order



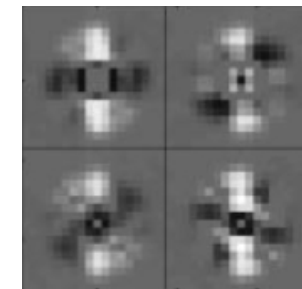
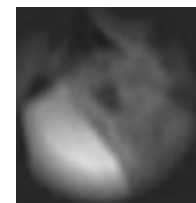
Volterra kernel estimation :



Phase-separated Fourier model:



Phase-separated Fourier model:



$h(\omega_x, \omega_y, \phi, \tau)$

(Fournier et al, 2011)

(David et al, 2004)

# RF estimation limitations

- Limited expressiveness of the fitted models
- Fitting to narrow stimulus statistics



- Limited prediction power
- Non unique estimation of the RF
- Poor interpretability in terms of underlying biological substrate

# What can we do about it?

1. Introduce domain knowledge:

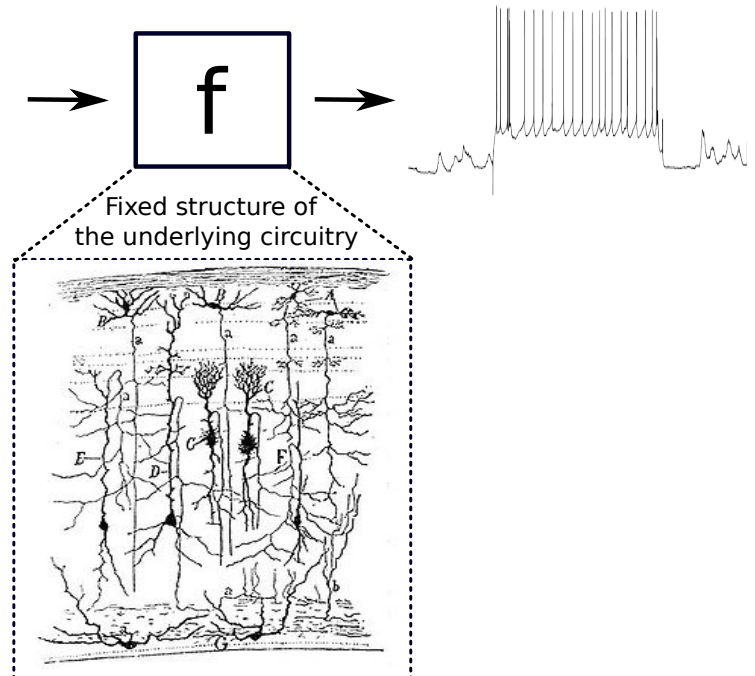
more priors = better and less biased fit

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1. Introduce domain knowledge:

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2. Think of the underlying biological substrate

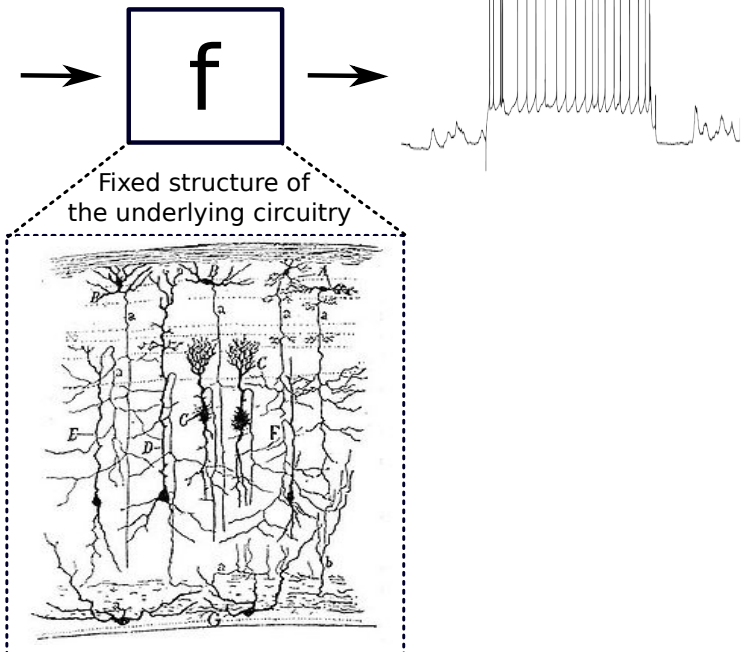


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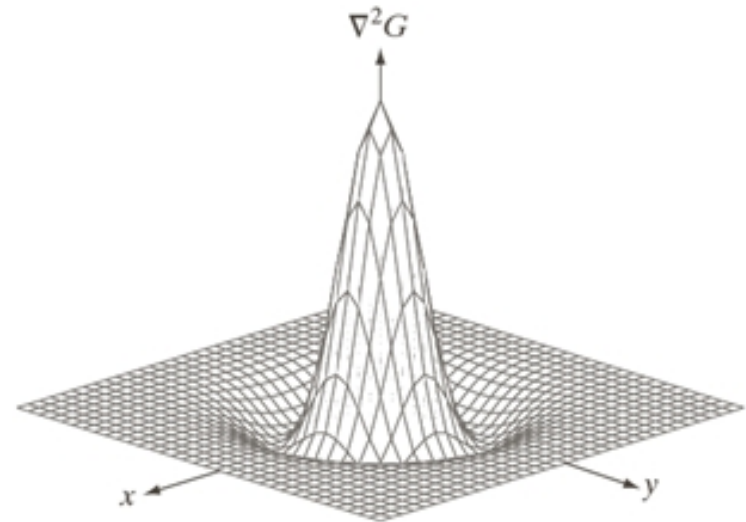


1+2 : Use knowledge about the architecture of the underlying neural circuitry as prior for your model.

# Hierarchical structural model (HSM)

# The structural priors

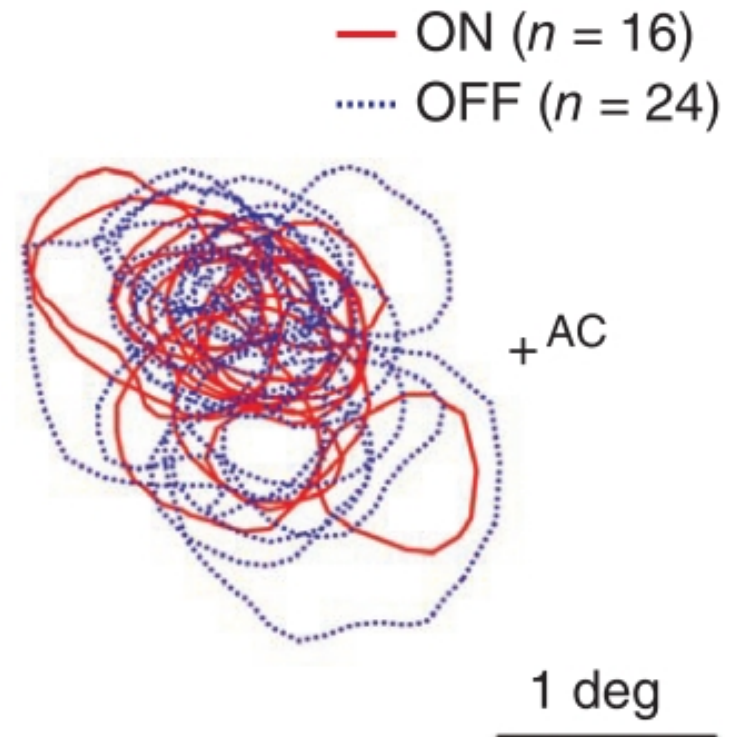
- Receptive fields of LGN units can be well approximated by difference-of-Gaussian function





# The structural priors

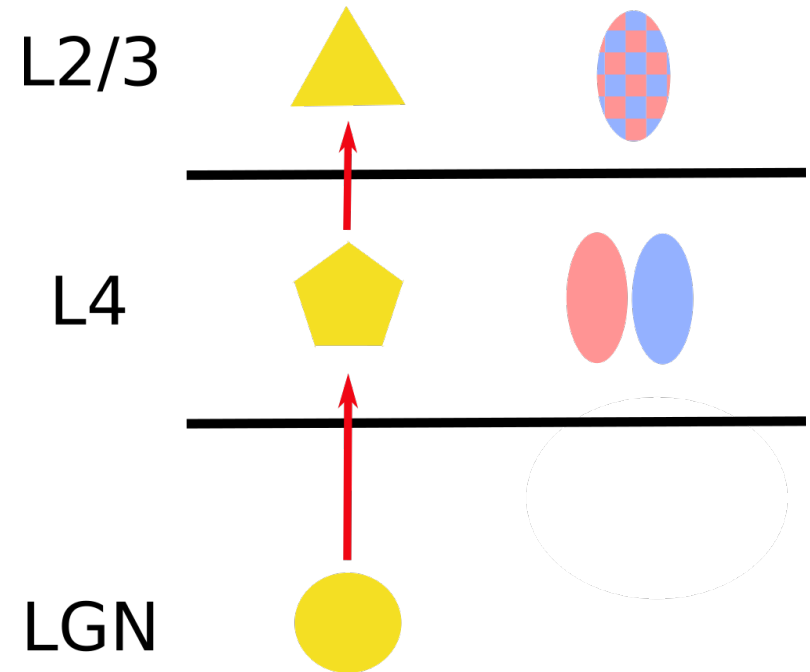
- Receptive fields of LGN units can be well approximated by difference-of-Gaussian function
- Local population of V1 neurons receives common input from limited number of LGN cells



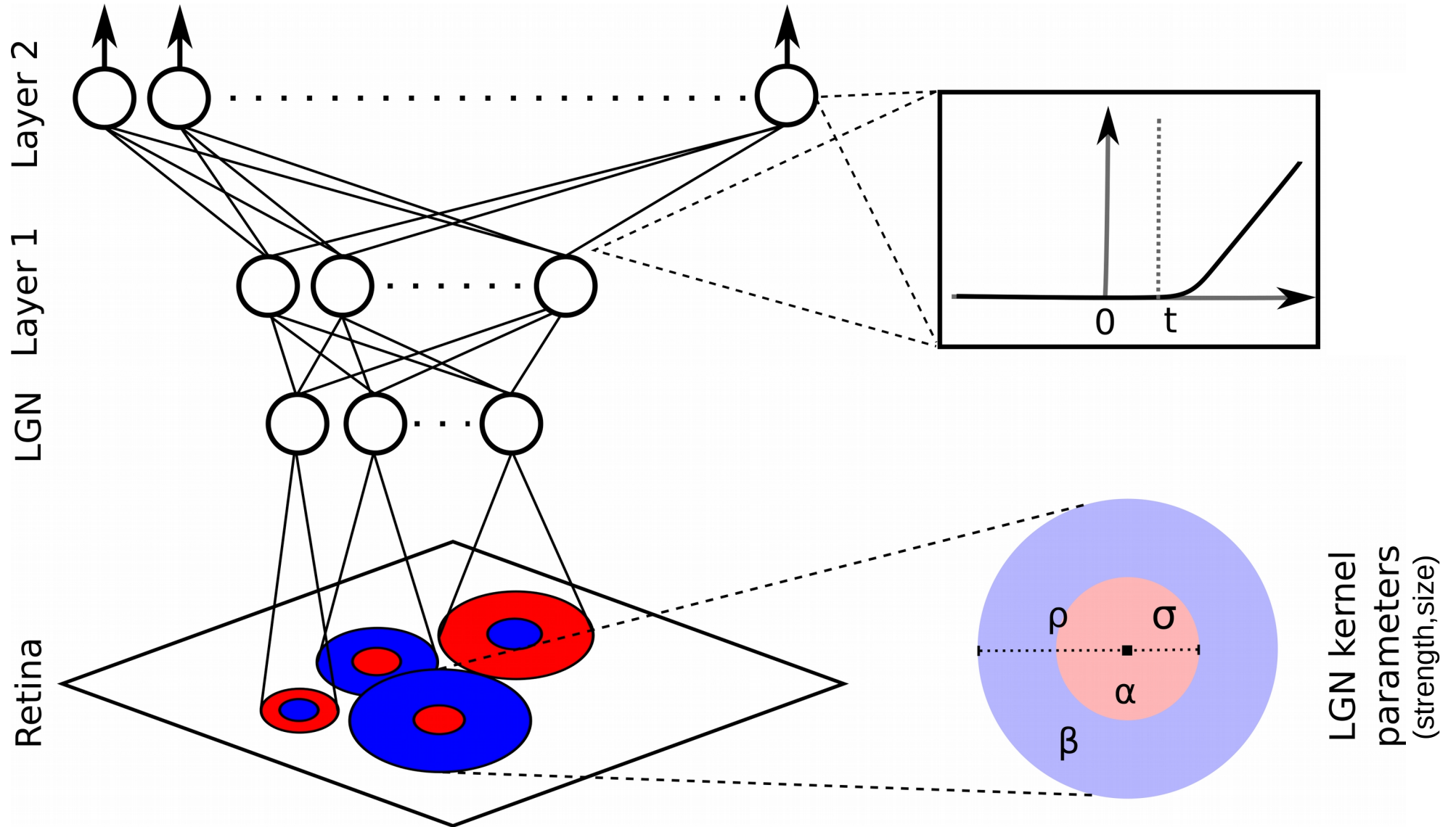
(Jin et al, 2011)

# The structural priors

- Receptive fields of LGN units can be well approximated by difference-of-Gaussian function
- Local population of V1 neurons receives common input from limited number of LGN cells
- Hierarchical organization



# The HSM structure



# The model

LGN units:

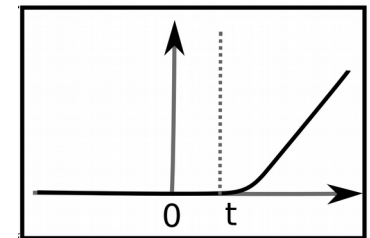
$$\psi_{il} = \sum_{k,l} I_{kl} \left( \frac{\alpha_i}{\sigma_i^2} e^{-\frac{(k-\mu_i^x)^2 + (l-\mu_i^y)^2}{2\sigma_i^2}} - \frac{\beta_i}{\rho_i^2} e^{-\frac{(k-\mu_i^x)^2 + (l-\mu_i^y)^2}{2\rho_i^2}} \right)$$

Cortical units:

$$\psi_{il} = f \left( \sum_j w_{ij} \psi_{j(l-1)} \right)$$

Transfer function:

$$f(x) = \log(1 + \exp(x - t_i))$$



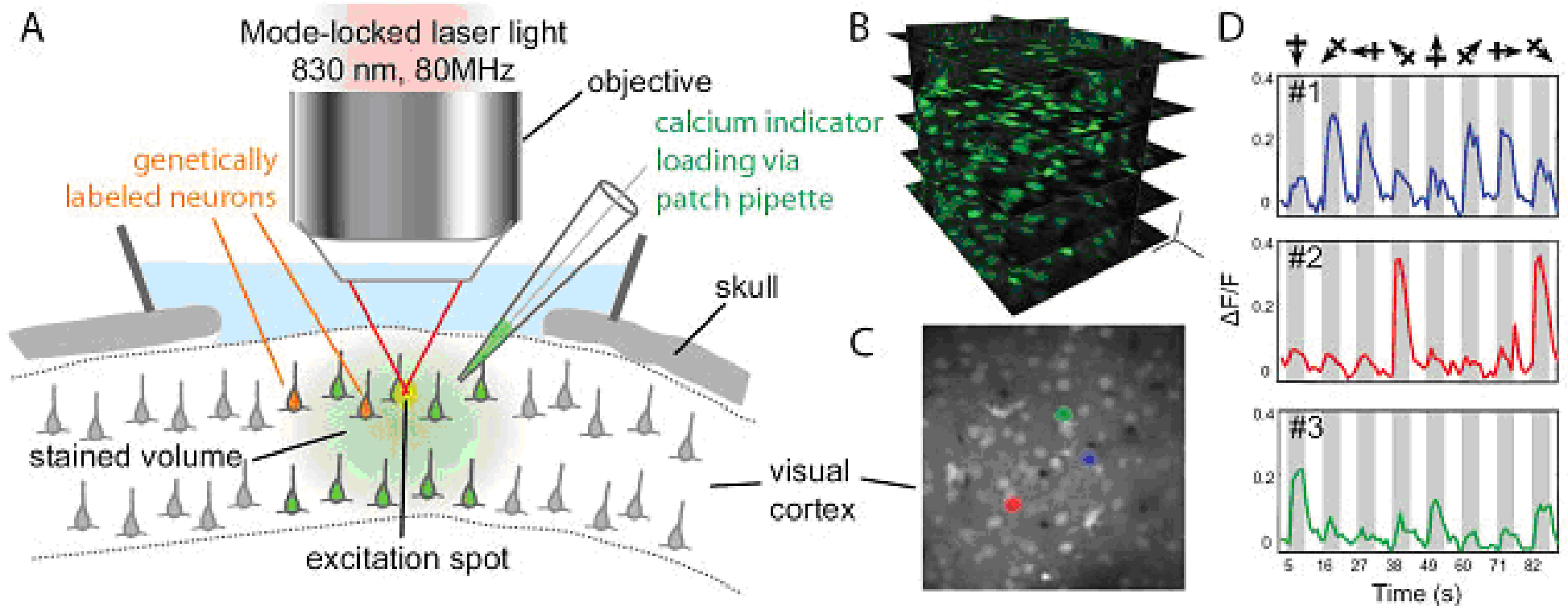
Log-likelihood:

$$\log p(y|x, \phi) = \sum_i y_i \log M(\phi, x_i) - \sum_i M(\phi, x_i)$$

# Model optimization

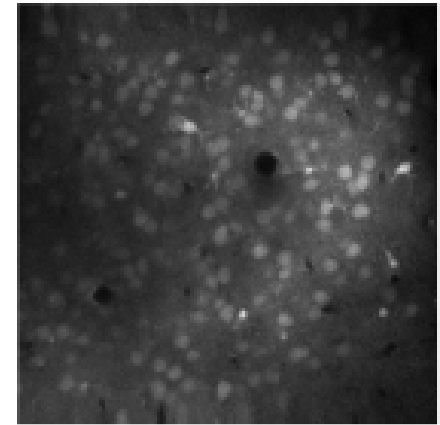
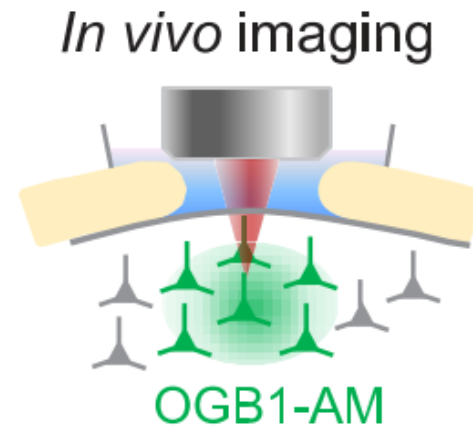
- Optimized with Constrained Truncated Newton Conjugate method
- Non-convex model
  - 100 restarts with different seeds of initial random parameter initialization
  - pick the best fit to **training** data
- Meta-parameters:
  - Number of LGN units (9)
  - Number of hidden units (20%)
  - Determined based on prior 1D searches based on **training** data performance

# 2-photon imaging of neural populations



# Calcium imaging of local population of neurons in mouse V1

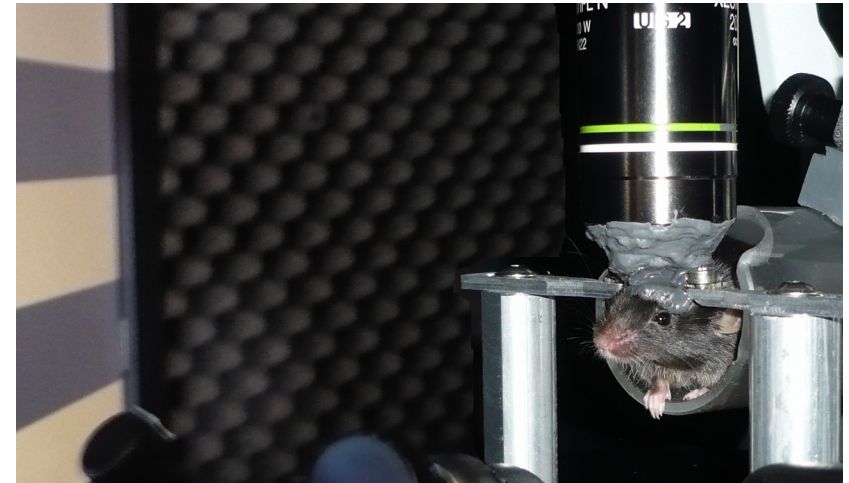
- 2 mice, 30-40 postnatal day
- Anesthetized: isoflurane
- 3 imaged regions
- OGB1-AM calcium indicator



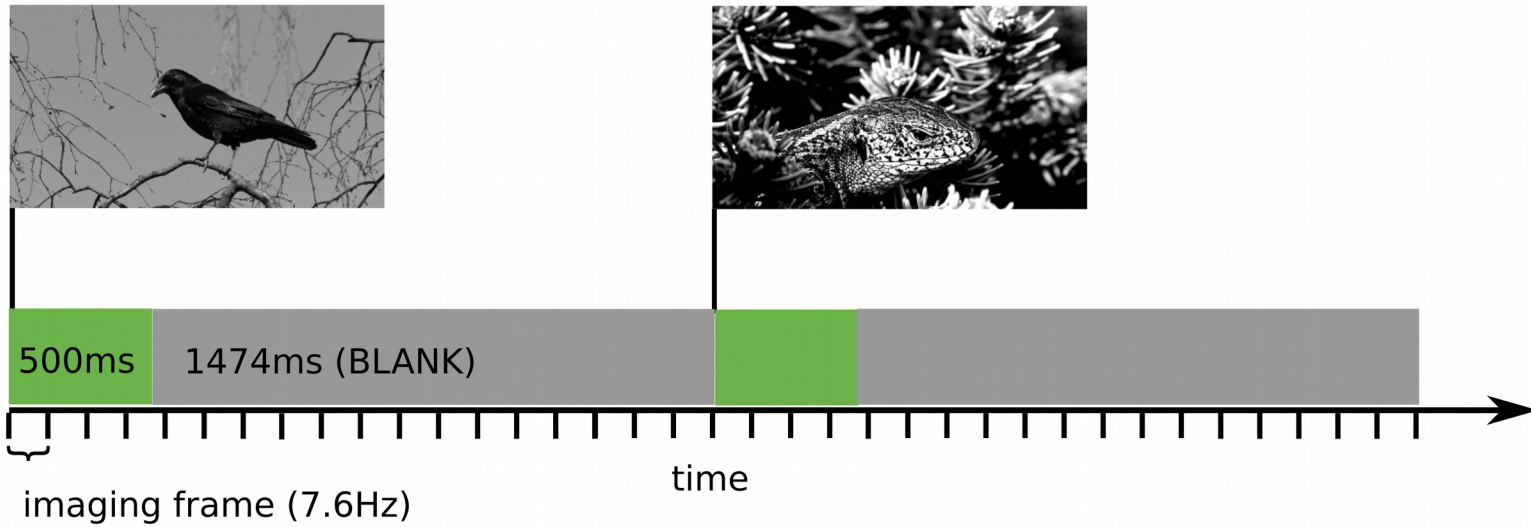
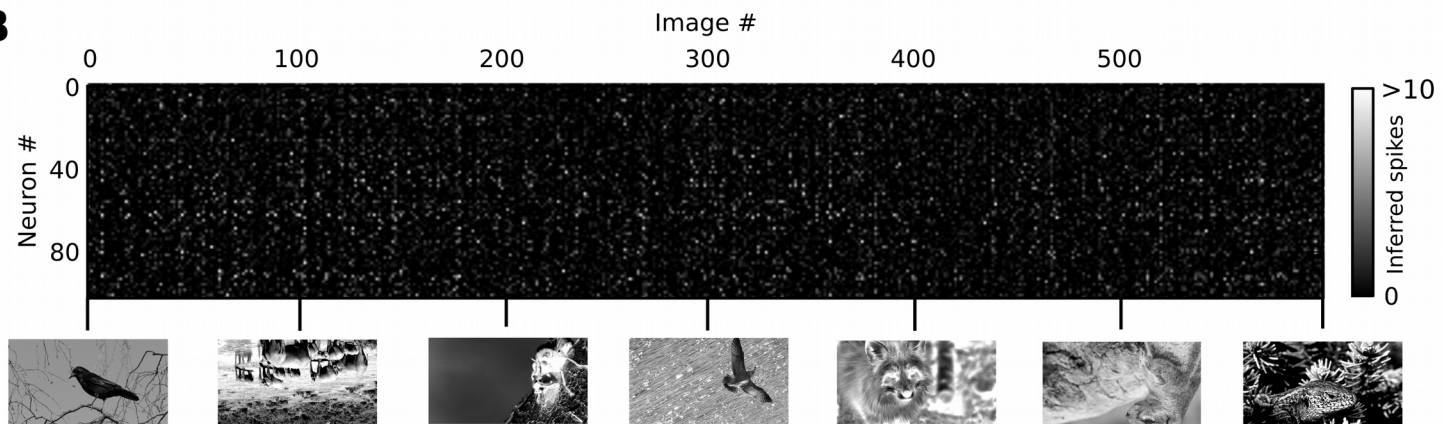
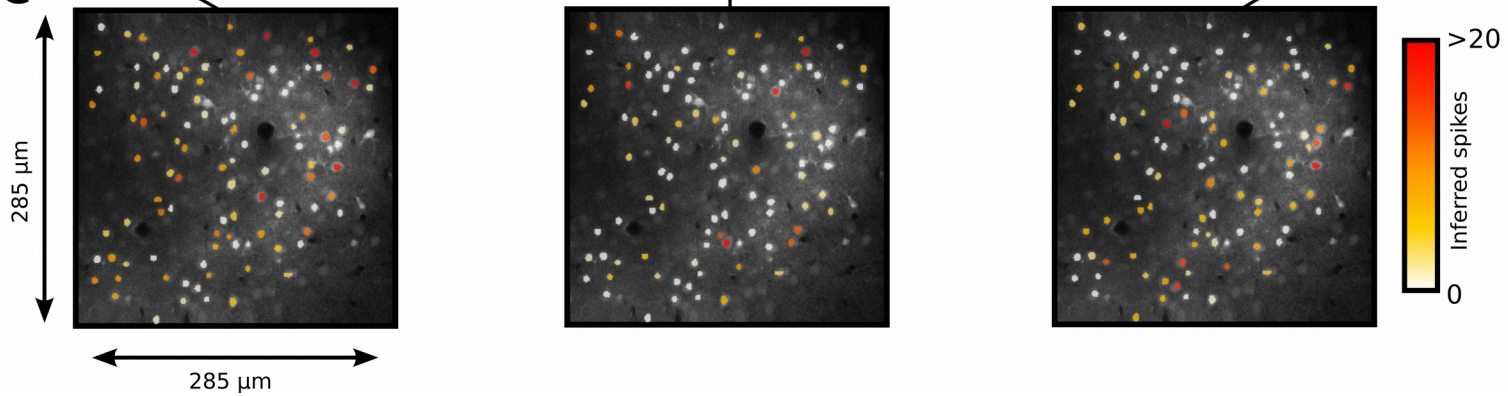
Sonja Hofer



Thomas  
Mrsic-Flogel





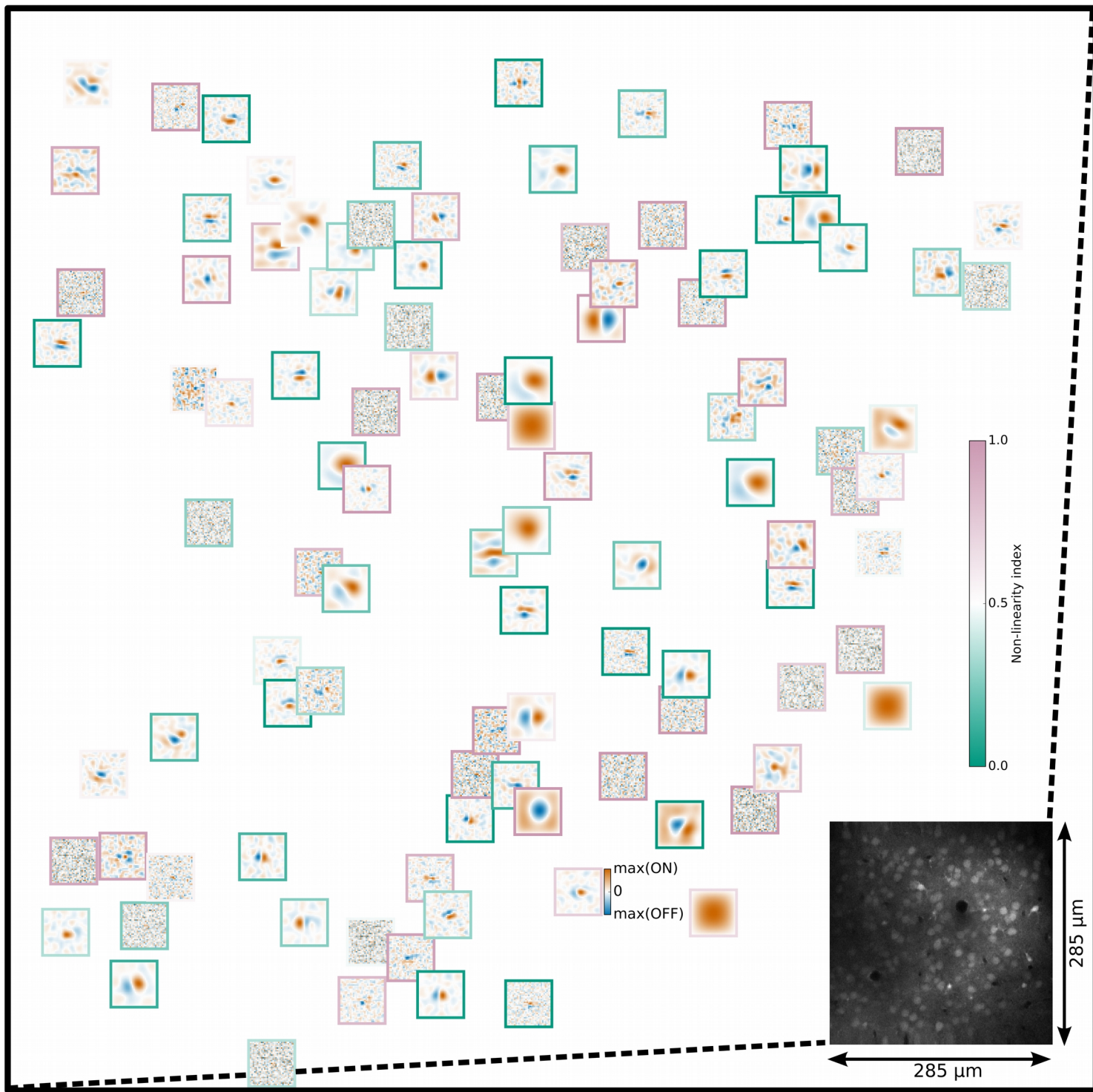
**A****B****C**



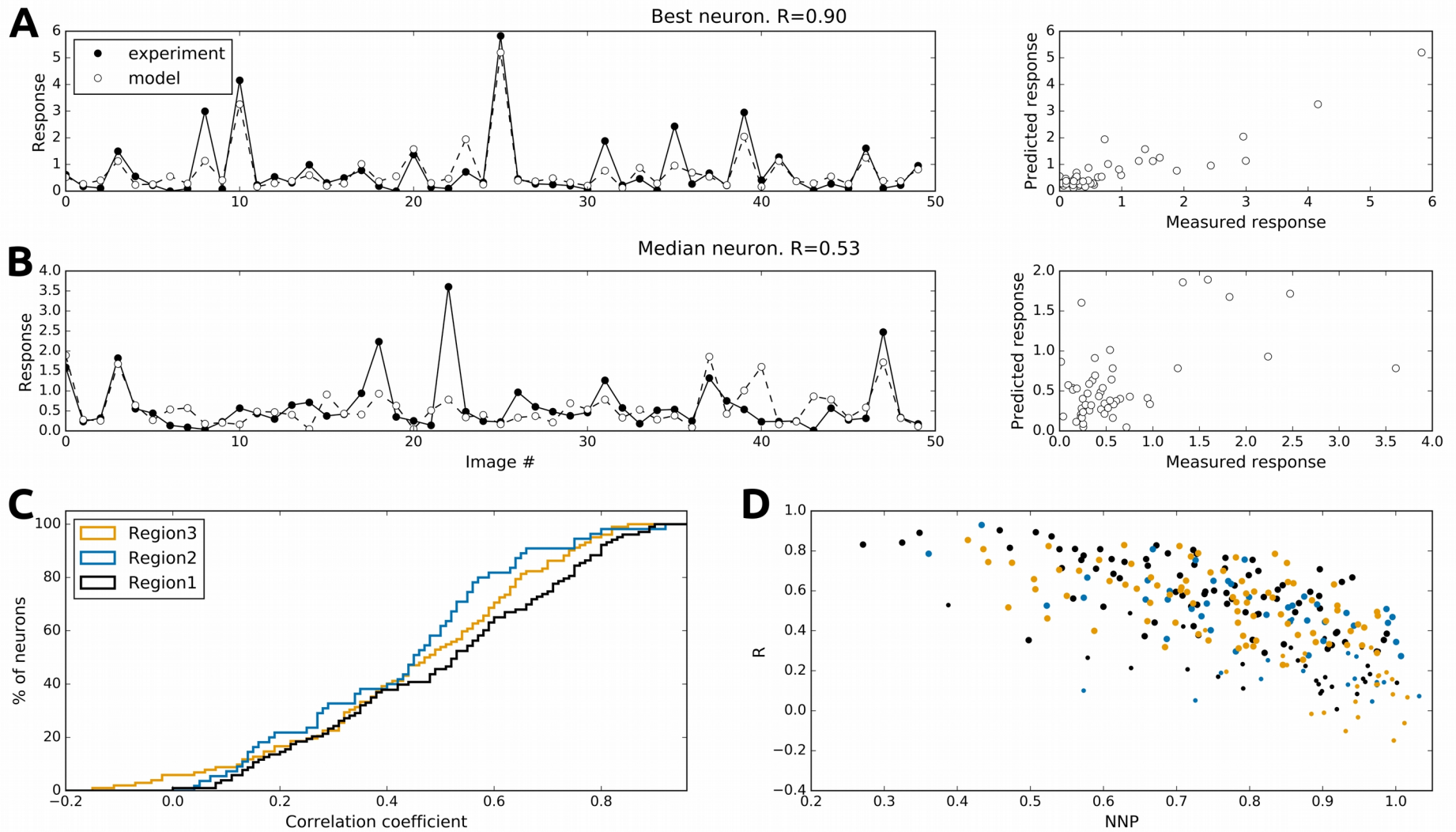
# The recordings

- 3 imaged regions in 2 mice
- 257 neurons in total
- Training set: 1260-1800 images 1 trial
- Validation set: 50 images 8-12 trials

# Results



# The model performance



# Comparison: reference models

STA with laplacian regularization  
(Smyth et. al, Journal of Neuroscience, 2003)

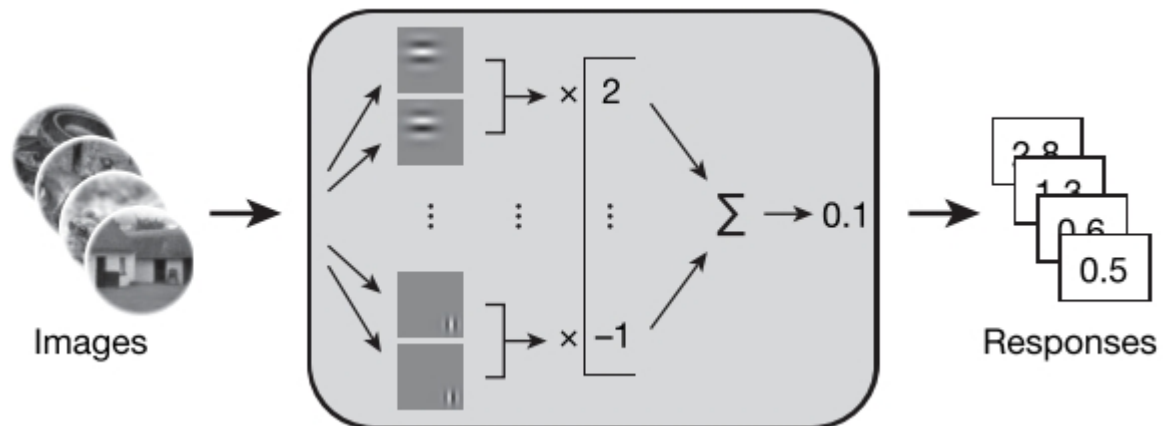
$$\mathbf{L}_s = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{bmatrix}. \quad \begin{bmatrix} \mathbf{S} \\ \lambda \mathbf{L} \end{bmatrix} \mathbf{f} = \begin{bmatrix} r \\ 0 \\ \vdots \\ 0 \end{bmatrix},$$

# Comparison: reference models

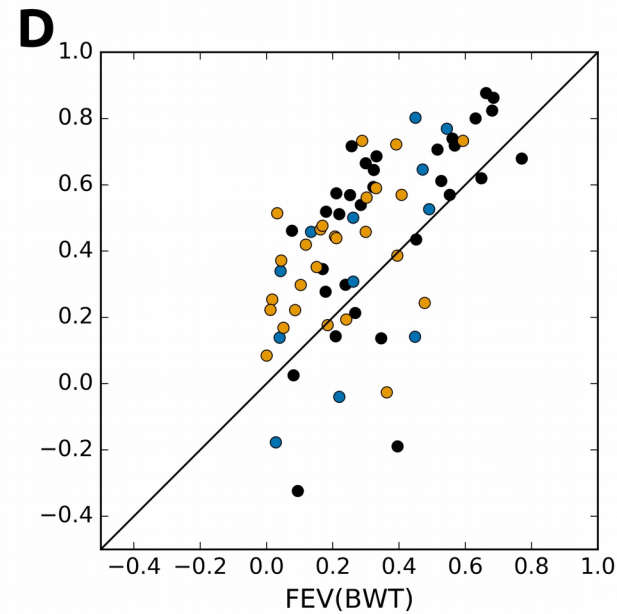
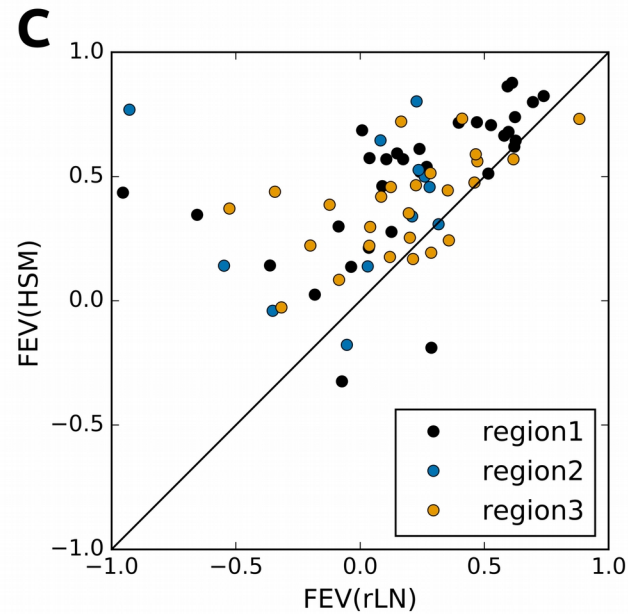
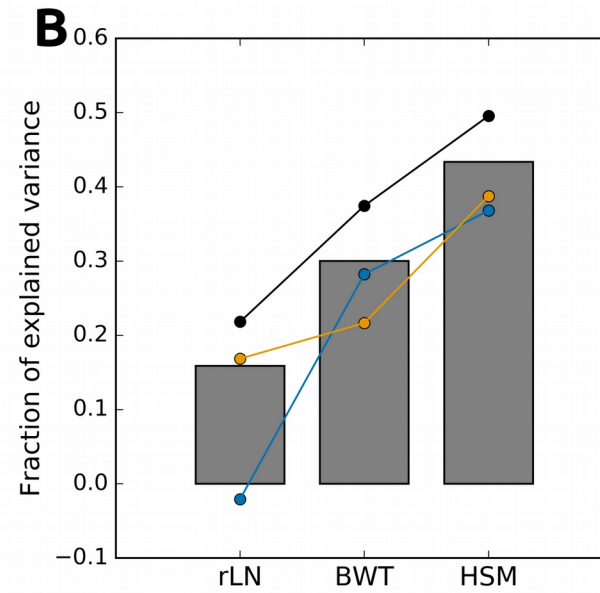
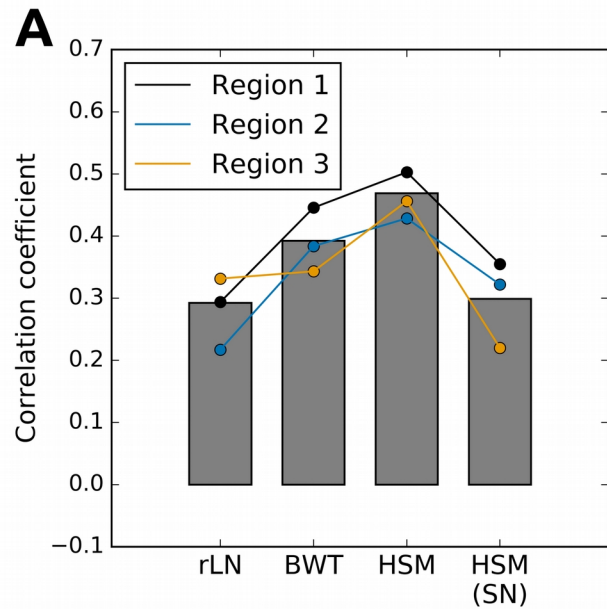
STA with laplacian regularization  
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Barkely-wavelet transform based linear model  
(Kay et. al, Nature, 2008)



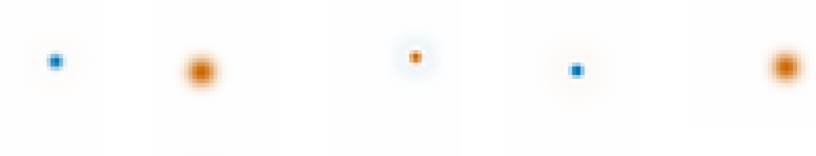
# Comparison: performance



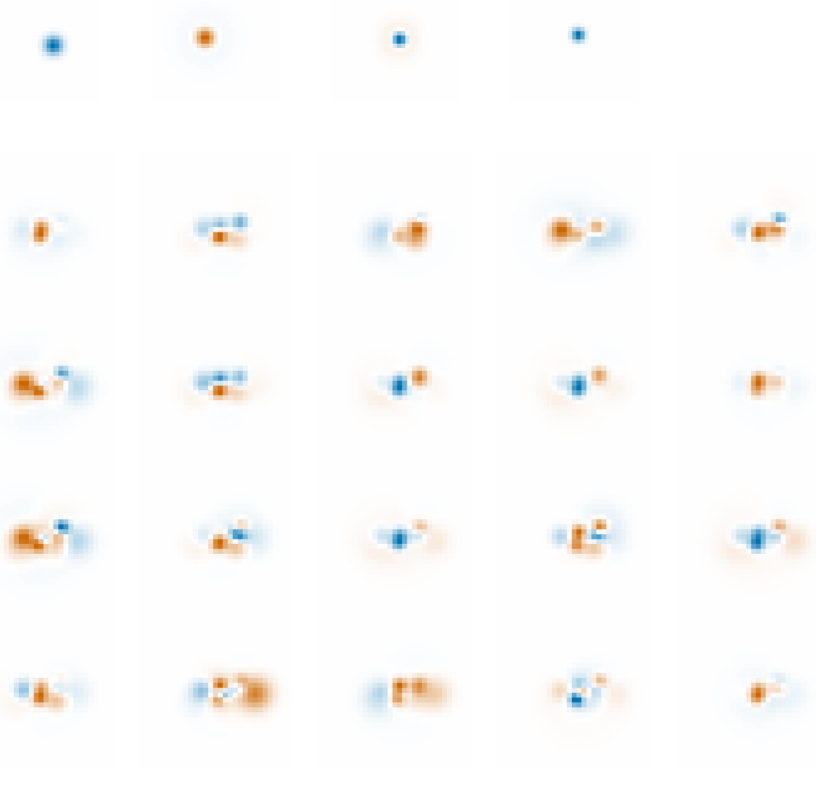
# Fitted HSM weights

Region 1

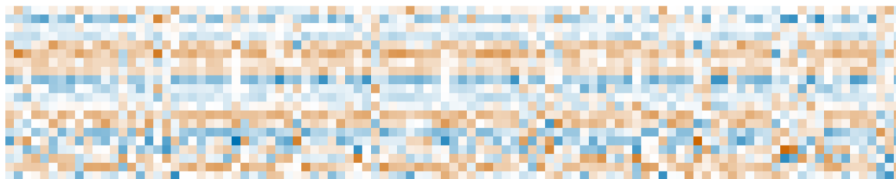
LGN RFs



Hidden  
layer  
RFs



Output  
layer  
weights





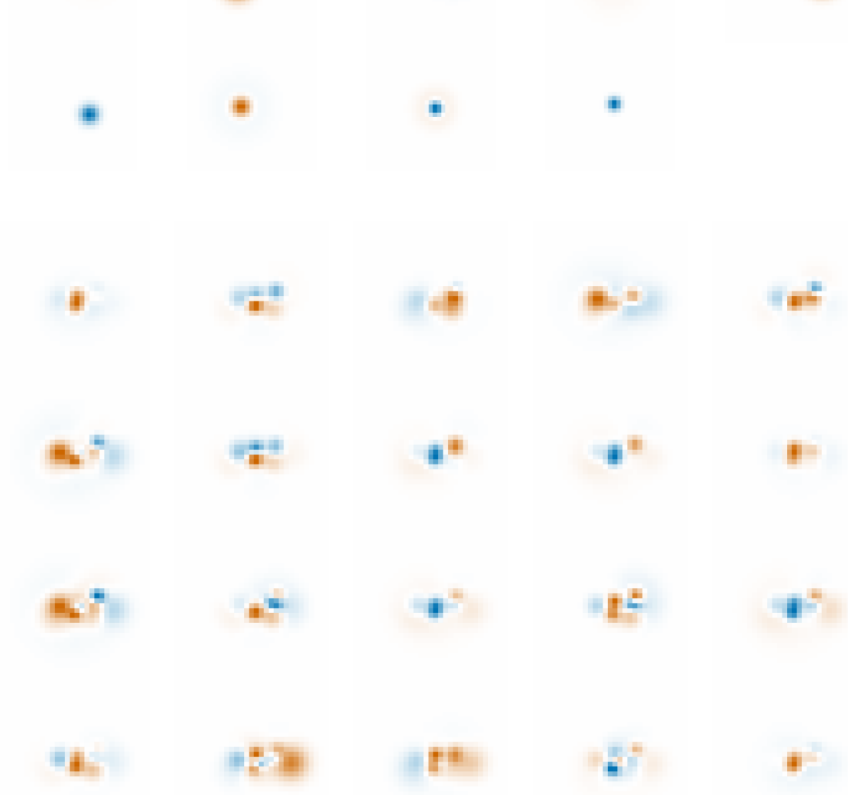
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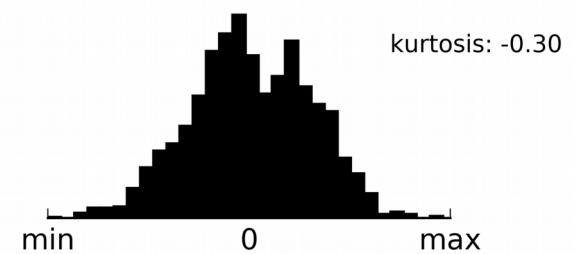
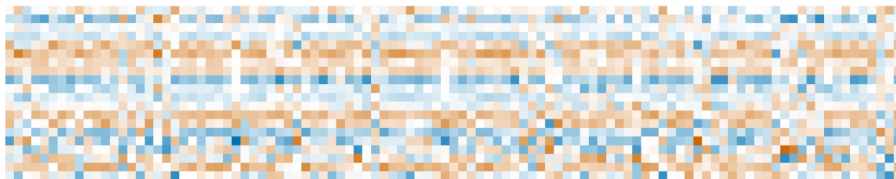
LGN RFs



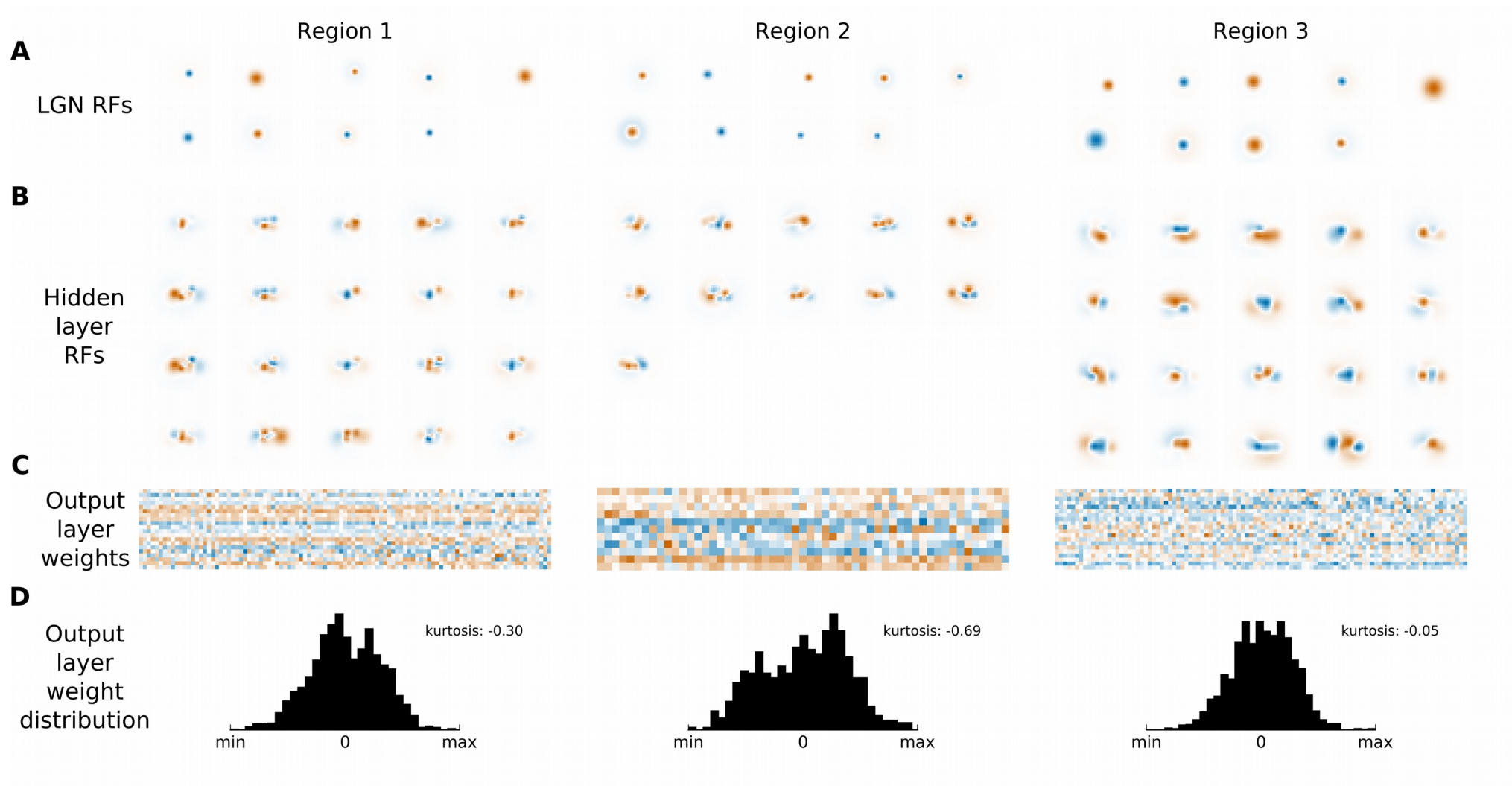
Hidden  
layer  
RFs



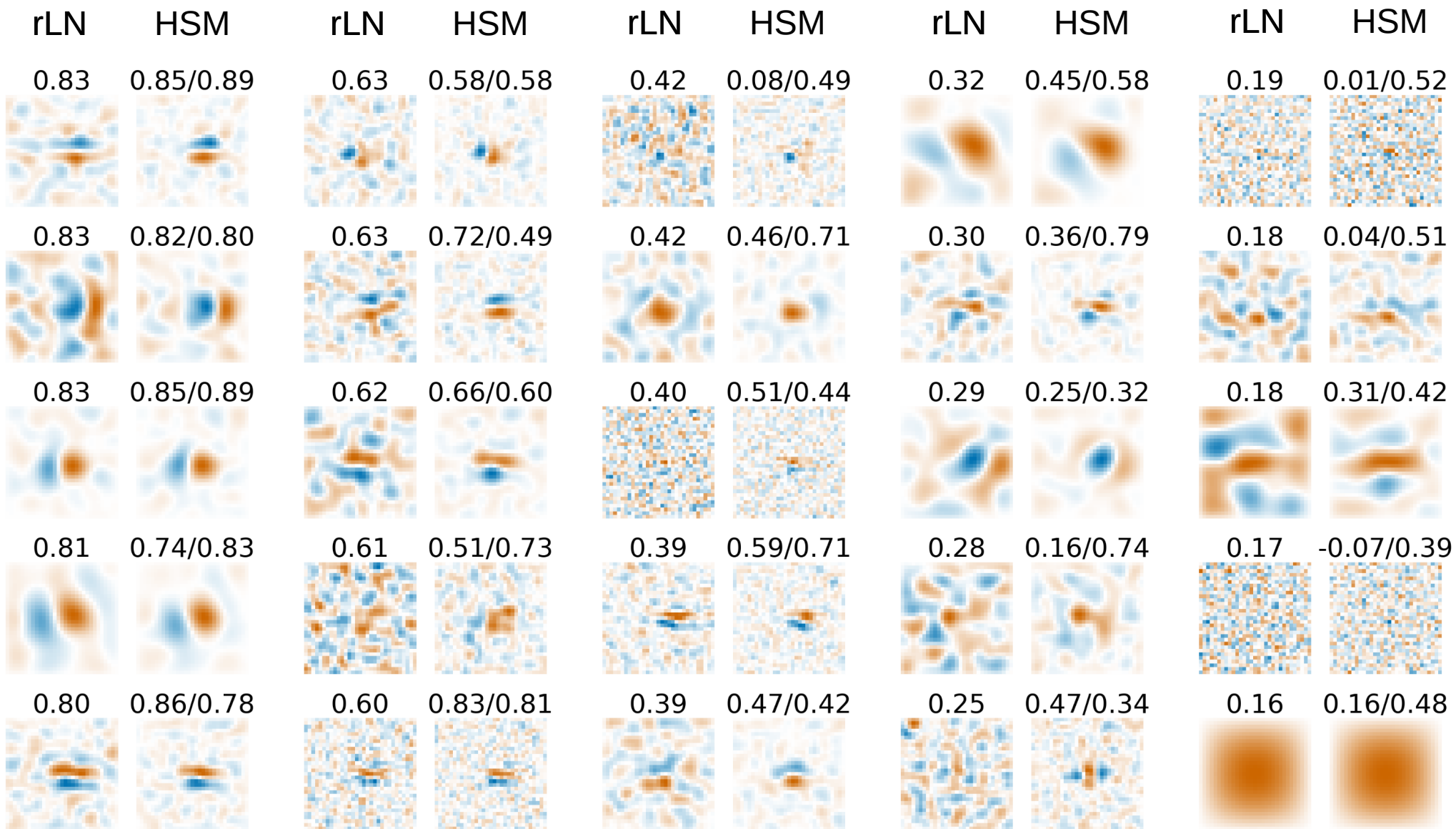
Output  
layer  
weights



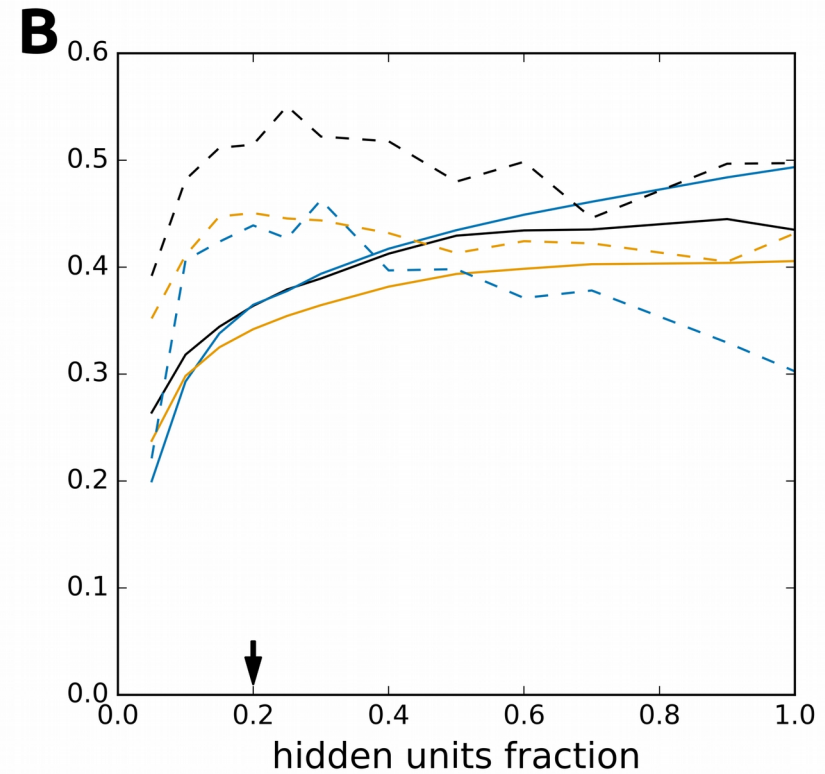
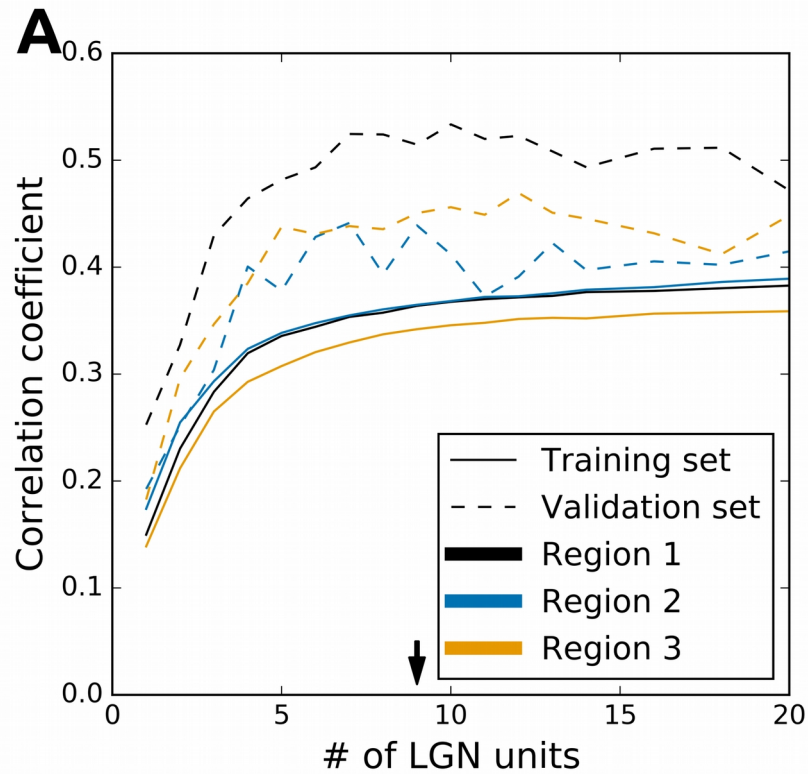
# Fitted HSM weights



# RF comparison across models



# Metaparameters



# Conclusions

- Introduction of cortical architecture into model leads to more accurate prediction of population responses to natural images
- Significant reduction of free parameters compared to many competing models
- Diverse set of receptive fields in local population of mouse V1 neurons can be constructed from surprisingly few LGN-like units
- Can systematic introduction of prior knowledge about the thalamo-cortical circuitry lead to better correspondence between fitted models and underlying neural substrate, and thus save the RF?

# Future work: better calcium imaging systems

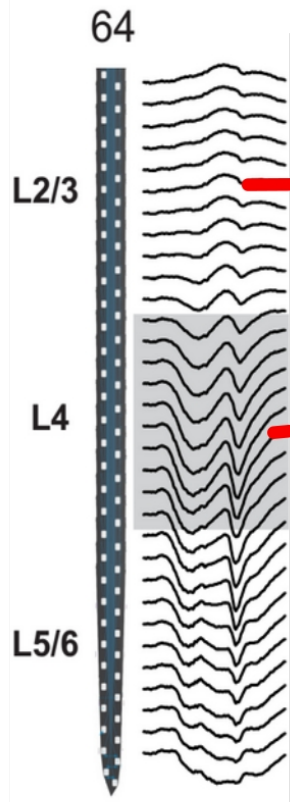
- Widefield objective = more simultaneously recorded cells
- Chronic preparation = more image presentations
- Deeper recordings = more available priors
- New dyes = less noise, single spike resolution
- Faster scanning frequency
- Recordings combined with neuronal markers

# Future work: model extensions

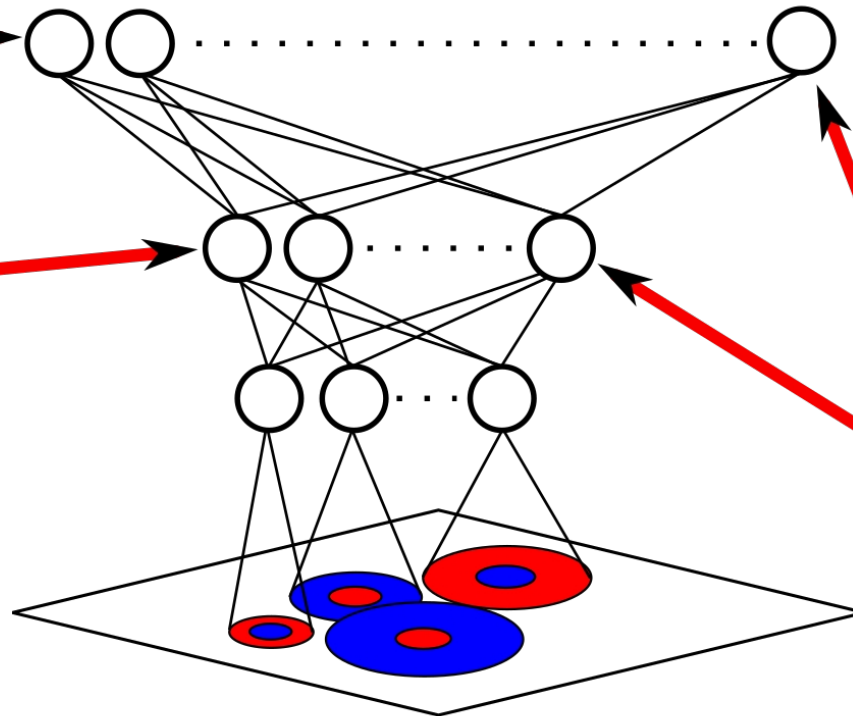
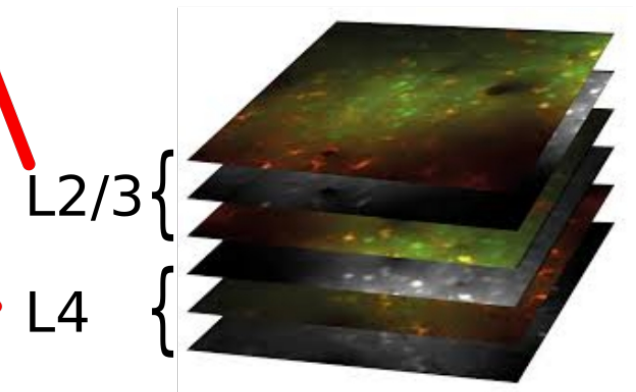
- Temporal receptive fields to fit natural scenes animations
- Stimulus dependent surround contributions, with explicit priors about structure of lateral connectivity
- Coupling filters between cortical neurons (a.k.a. GLM)
- Adaptive mechanisms
- Separate excitatory and inhibitory neurons
- Explicit handling of ongoing-state
- Trans-laminar model fitting

# Trans-laminar model fitting

Trans laminar electrode array



Two-photon calcium imaging



Cyril Monier



Margot Larroche



Thomas Deneux

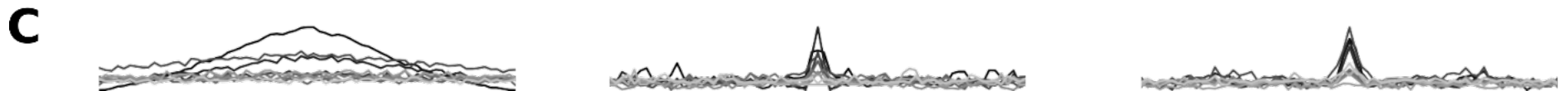
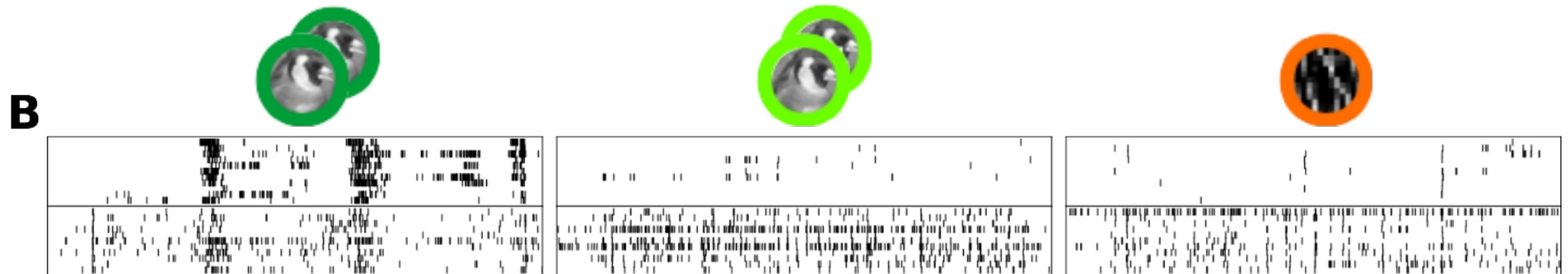
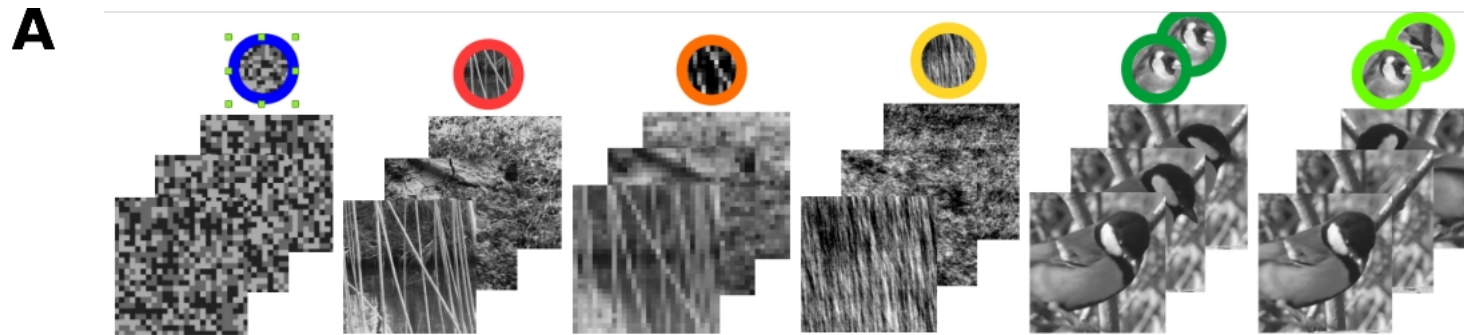


Brice Bathellier

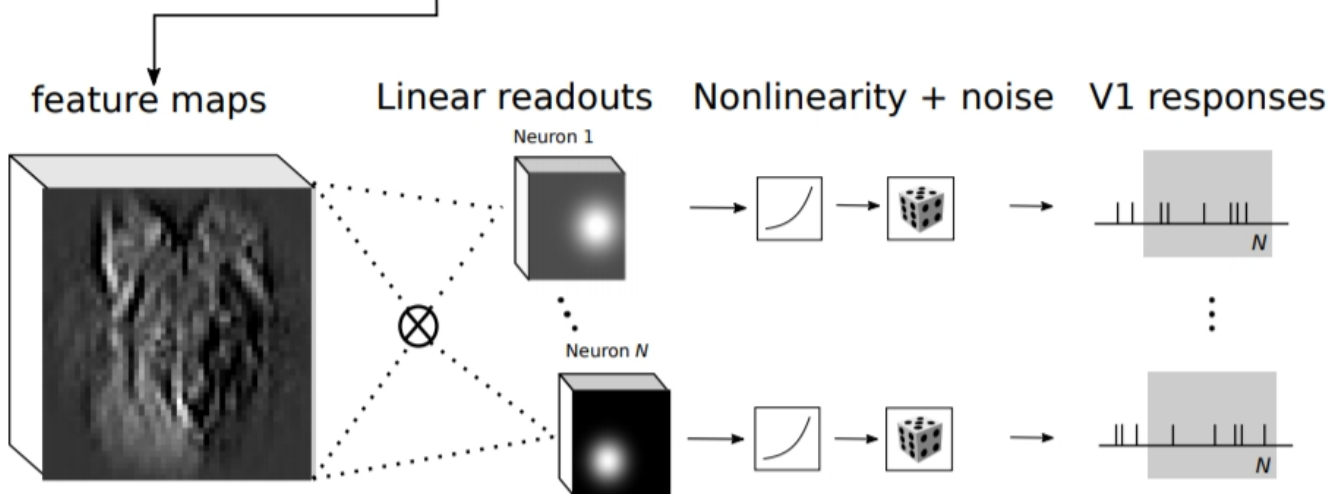
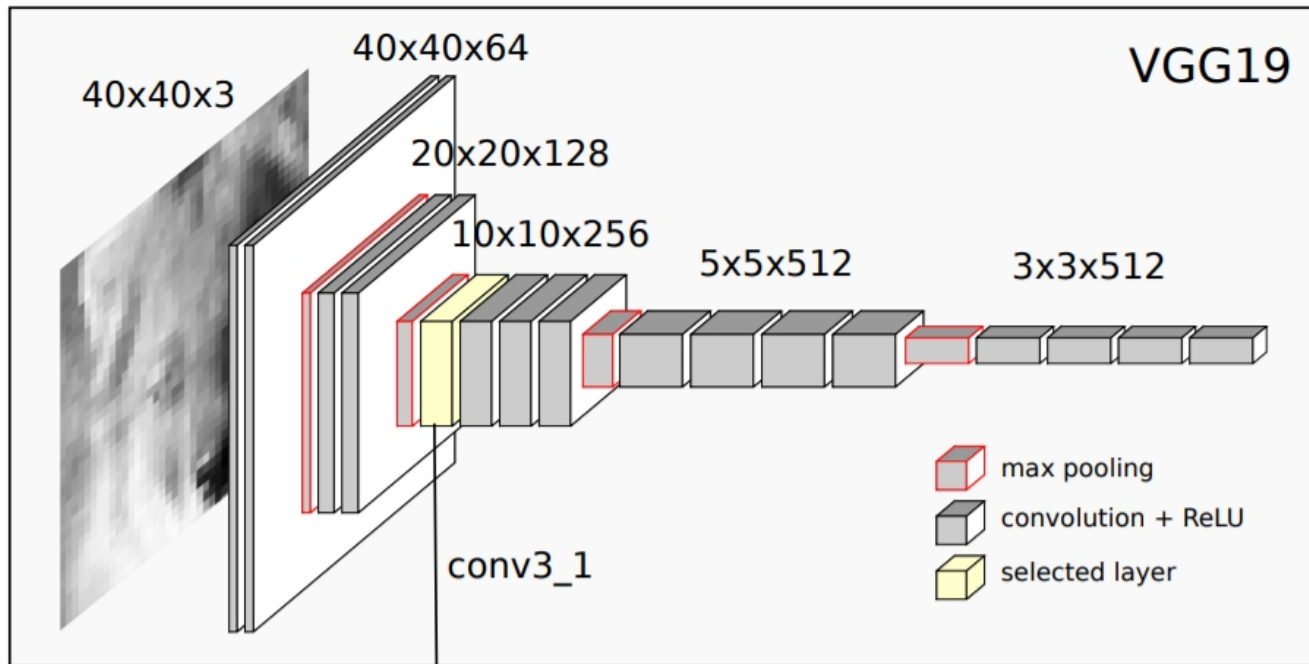




# Exploration of different image statistics (adaptation?)



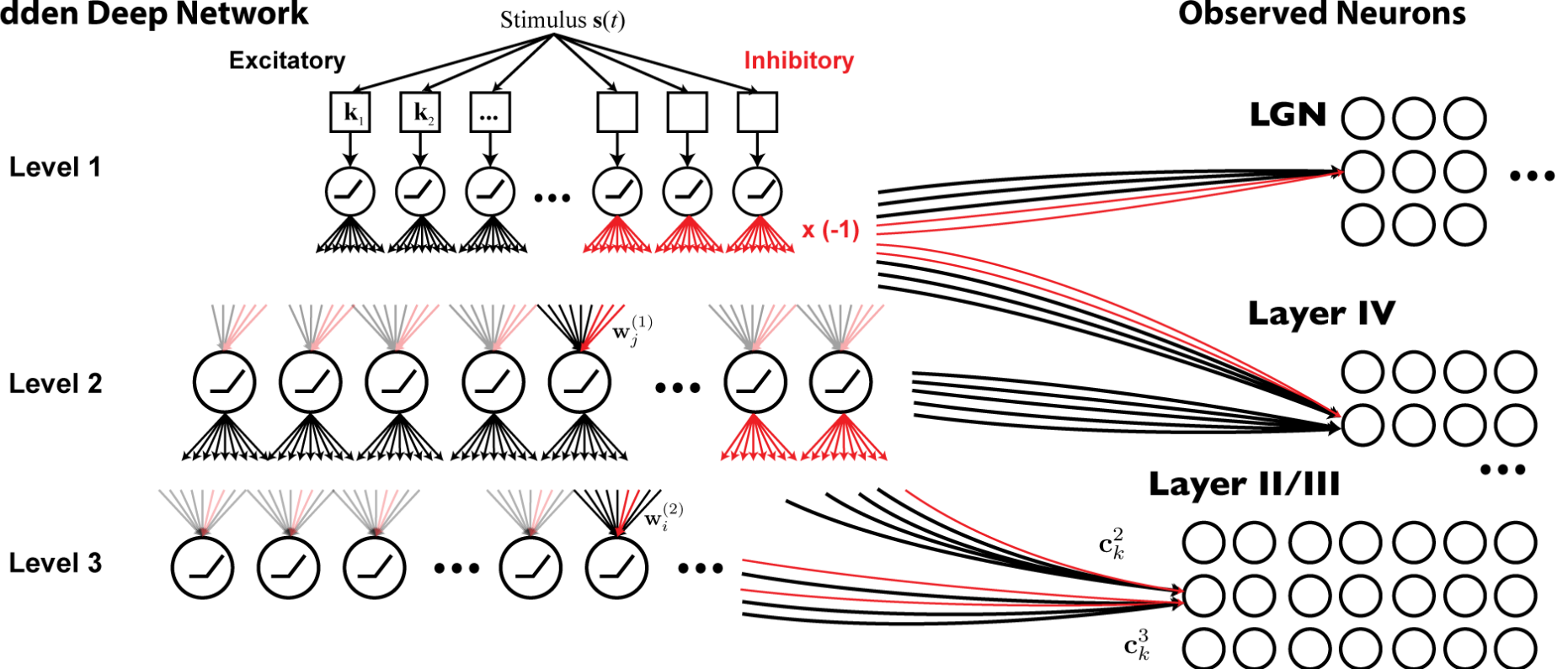
# Recent entry of CNNs into neuroscience



# New Deep Architectures

## Hidden Deep Network

## Observed Neurons

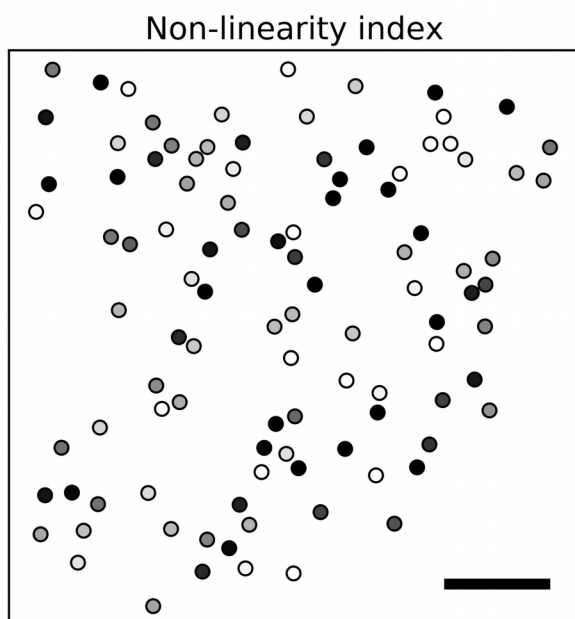
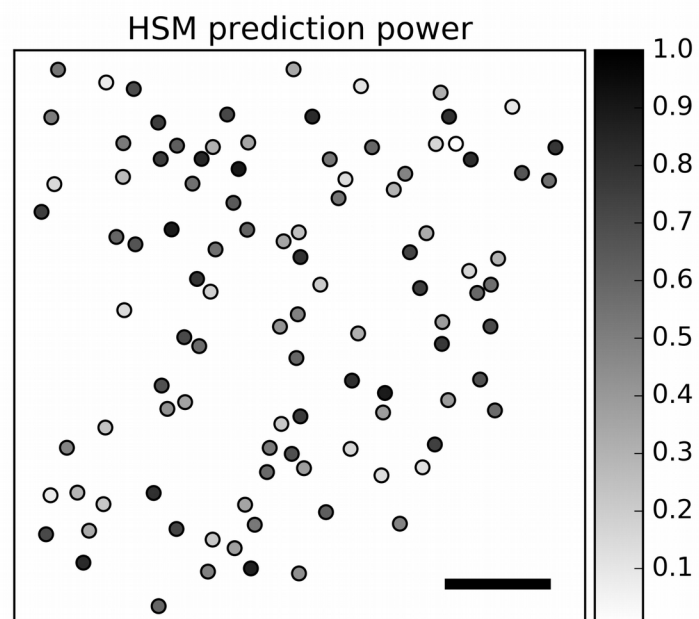
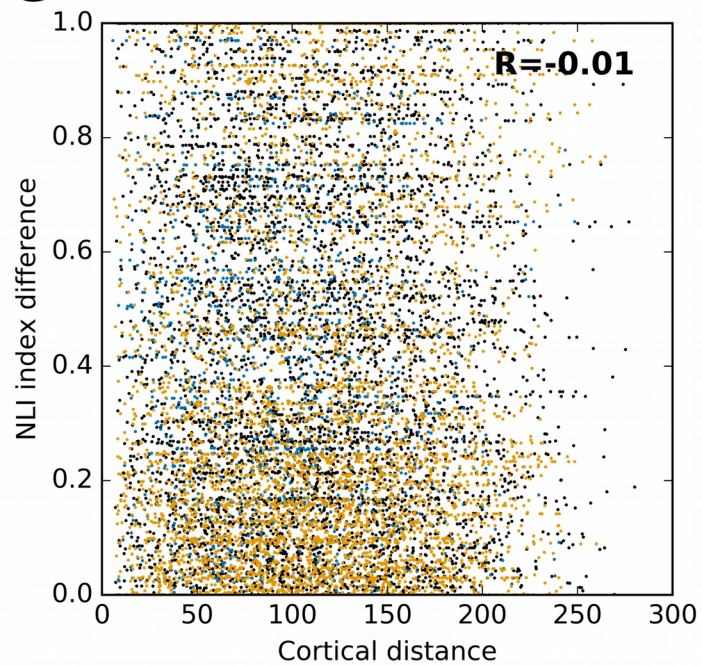
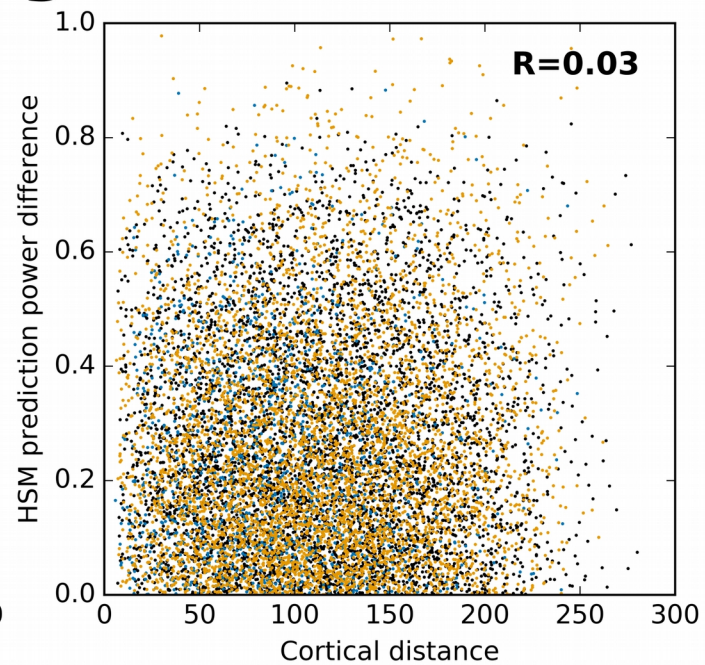


Dan Butts, Univ. of Maryland

THE END

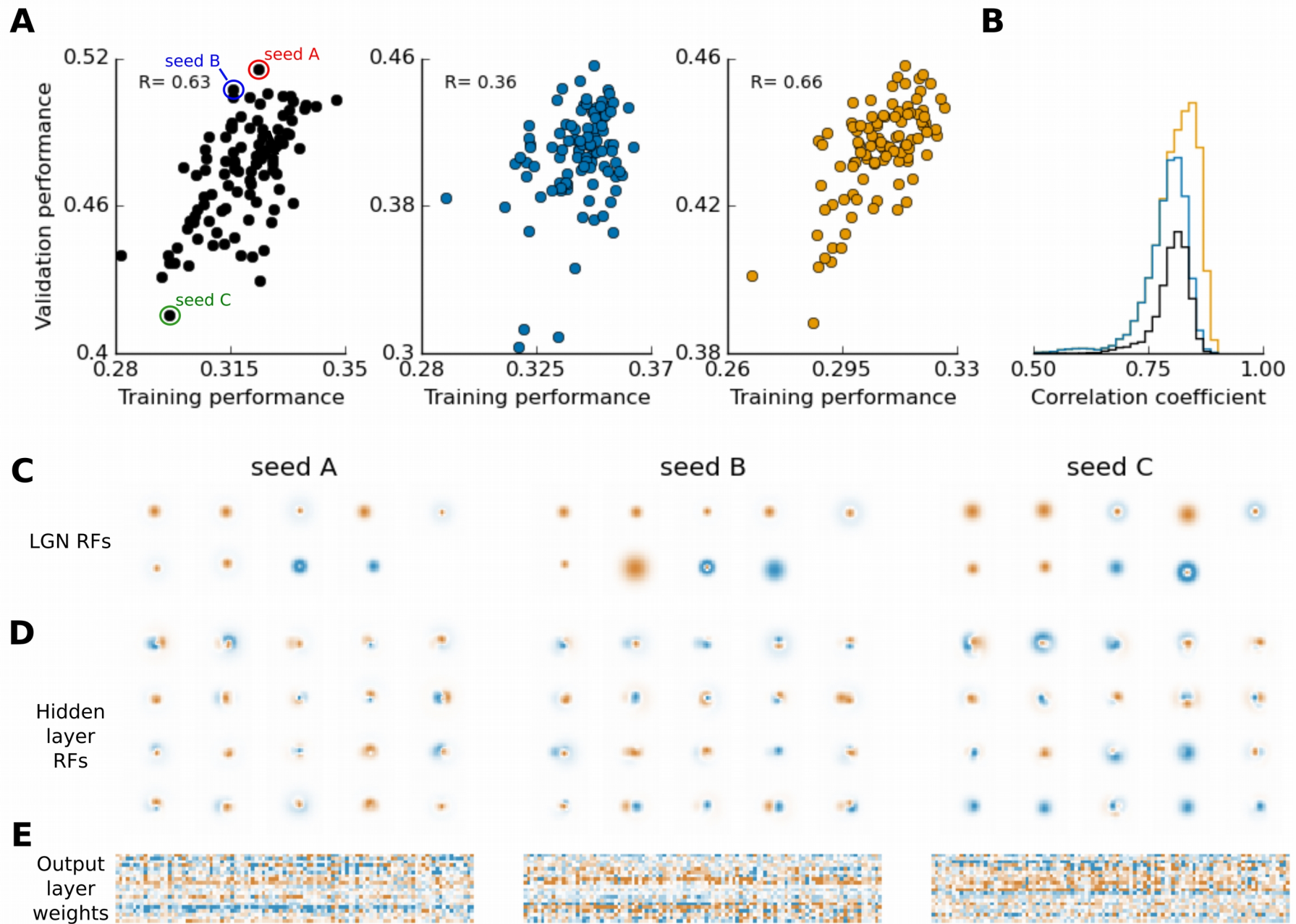
WE ARE ALWAYS LOOKING FOR  
TALENTED STUDENTS



**A****B****C****D**



# Dependence on initialization seed



# Dependence on data resampling

